Problems (AC)

[1] A 200V, 50Hz supply is connected to coil of inductance (0.15H) connected in Series with 32Ω resistance

Determine
① impedance of the Circuit.
② Current & circuit phase angle.
③ Pd (potential difference) ~~Power dissipated~~ across 32Ω.
④ " " " coil.

← Solution →

(a) $Z = R + j\omega L$

$= 32 + j(2\times\pi\times 50\times 0.15)$

$= 32 + j\underbrace{47.1}_{X_L} \quad = 57\angle 55.81^\circ$

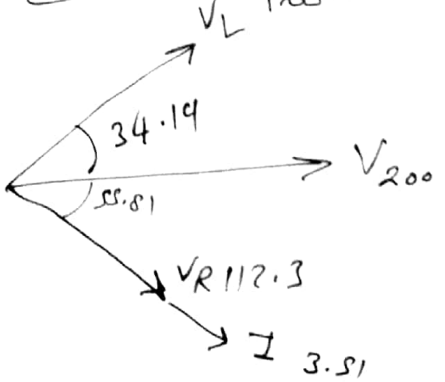
(b) $I = \frac{V}{Z} = \frac{200\angle 0}{57\angle 55.81} = 3.51\angle -55.81^\circ$

(c) $Pd|_{32\Omega} = V_R = IR = (3.51\angle -55.81)(32\angle 0)$

$= 112\angle -55.81^\circ$

(d) $Pd|_{coil} = V_L = I X_L = (3.51\angle -55.81)(47.1\angle 90)$

$= 165.3\angle 34.19^\circ$



(3) << ابدأ بسؤال الأخير

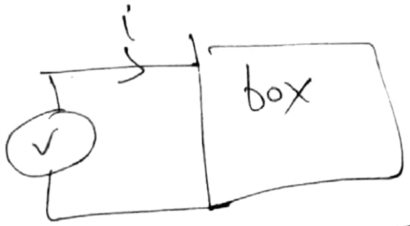
(4)

(ماسمى الأخير)

if $v = 2\sin(100t + 45^\circ)$

$i = \cos(100t + 10^\circ)$

what type of impedance in box



sol

$$Z = \frac{v}{I} = \frac{2\angle 45}{1\angle 100} = 2\angle -55$$

$\cos(wt + 10) \equiv \sin(wt + 90 + 10)$

$= 2\cos 55 - j\,2\sin 55$

R → capacitor $\frac{1}{wC} = 2\sin 55$

100

$\therefore C =$

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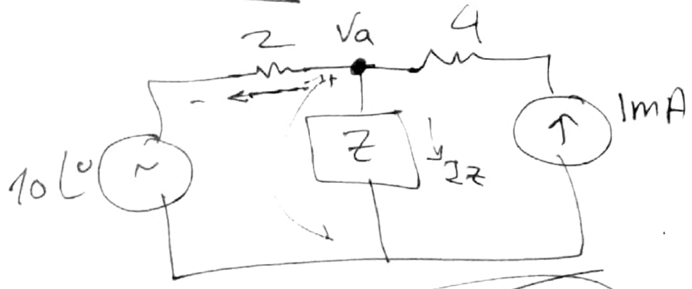
(3) find Z if $V_a = 14 - j2$



$\therefore V_a - 10\angle 0 = V_{2\Omega}$

$14 - j2 - 10 = V_2 = +4 - j2$

$\therefore i_2 = \frac{4 - j2}{2} = 2 - j1$

$i_Z + i_2 = 1\,mA$

$i_Z + 2 - j1 = 1\times10^{-3}$

$i_Z = j1 + 2 + 1\times10^{-3}$

$\therefore \frac{V_a}{I_Z} = \frac{14 - j2}{(2 + 0.001) + j}$

$= \frac{\square - \square j}{\square}$ ... $\square - \square j$

فكرة قصيرة

نعمل تيار في Z وجيب V_a

I_Z ومنها نطلع Z

I_Z مستمر 1mA

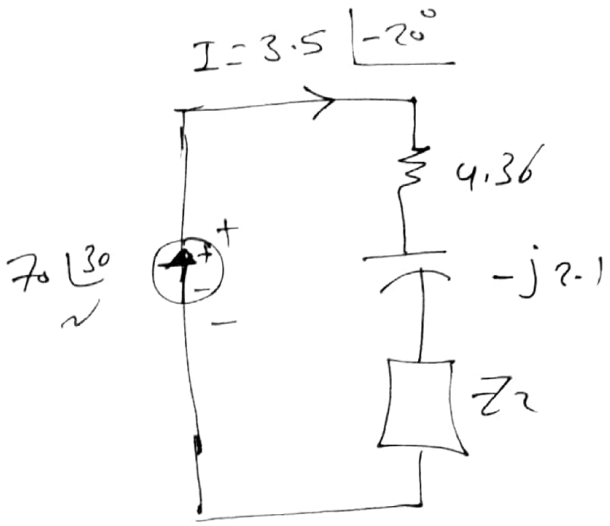
$V_2 + V_{supply}$

∴ يحتوي على R , C

معطوف في R

وبعض C منفصل أو معطوف

4 For the circuit shown determine Z_2



solution →

$$Z_{total} = \frac{V}{I} = \frac{70\angle 30}{3.5\angle -20}$$

$$= 20\angle 50$$

$$= 12.86 + j15.32\ \Omega$$

but

$$Z = Z_2 + \underbrace{(4.36 - j2.1)}_{R - j\frac{1}{\omega C}}$$

$$\therefore 12.86 + j15.32 = Z_2 + 4.36 - j2.1$$

$$Z_2 = 8.5 + j17.42 \quad \text{or} \quad 19.38\angle 63.99^\circ$$

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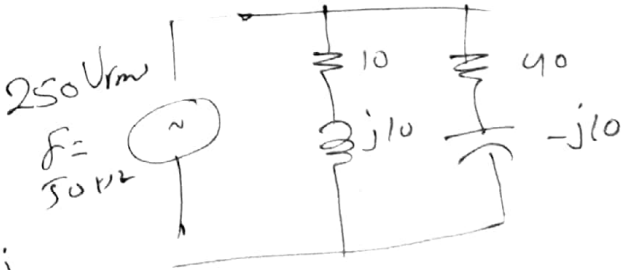
5 A series R-L branch with $R_1 = 10\Omega$, $L = 10\Omega$ connected in parallel with series RC branch of $R_2 = 40\Omega$, $X_c = 10\Omega$. The combination is connected across 250V (rms) supply, 50 Hz, find total impedance of circuit & total current (Magnitude & Phase).



$$Y_1 = \frac{1}{10 + j10} = \frac{10 - j10}{200}$$

$$= \frac{1}{20} - \frac{j}{20} = 0.05 - j0.05$$

$$Y_2 = \frac{1}{40 - j10} = \frac{40 + j10}{1600 + 100} = 0.023 + 0.008j$$

$$Y_t = Y_1 + Y_2 = 0.073 - 0.042j$$

$$= 0.857\angle -30.9$$

$$I = \frac{V}{Z_{eq}} = \frac{250\sqrt{2}\angle 0}{11.668\angle 30.9} = 30.3\angle -30.9$$

or 21.42 ∠ -30.9 rms

$$Z = \frac{1}{Y} = \frac{1\angle 0}{0.857\angle -30.9} = 11.668\angle 30.9$$

$$= 10.01 + j5.99$$

6) a series R-C ckt connected with AC sup with 100 Vrms & phase 45° at 50Hz, if the magnitude of capacitive element is half of the pure element, find Power factor

← sol →

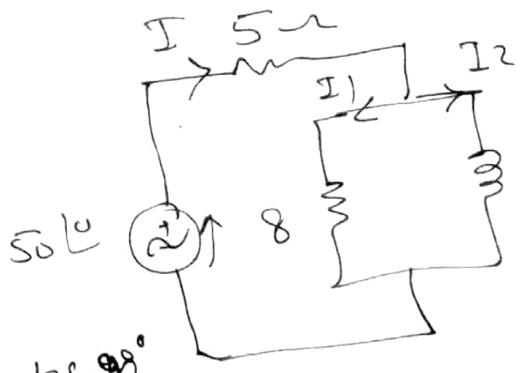
$Z = R - j\left(\frac{1}{\omega C}\right)$ $\quad pf = \cos\lfloor$ phase angle of Z

$\left|\frac{1}{\omega C}\right| = \frac{1}{2}|R| \quad \therefore \omega RC = \frac{1}{2}$

$pf = \cos\left[\tan^{-1}\frac{Img}{Real}\right] = \cos\left[\tan^{-1}\frac{-1}{\omega RC}\right]$

$= \cos\left[\tan^{-1}\frac{1}{2}\right] = 0.8944$

7) determine I, I_1, I_2



$Z_t = 5 + \frac{(8)(j6)}{8+j6} =$

$= 5 + \frac{48j[8-j6]}{(8)^2+(6)^2}$

$= 7.88 + j3.84\,\Omega$ or $8.77\lfloor 25.98°$

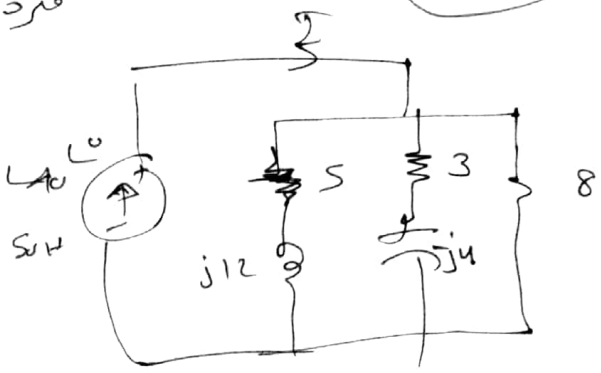
$I = \frac{V}{Z_t} = \frac{50\lfloor 0}{8.77\lfloor 25.98} = 5.7\lfloor -25.98°$

$I_1 = I\left(\frac{j6}{8+j6}\right) = 5.7\lfloor -25.98 * \left[\frac{6\lfloor 90}{10\lfloor 36.87}\right] = 3.42\lfloor 77.15°$

$I_2 = I\left(\frac{8}{8+j6}\right) = 5.7\lfloor -25.98 \left(\frac{8\lfloor 0}{10\lfloor 36.87}\right) = 4.56\lfloor -62.85$

(5)

(8) For the Parallel network shown find I



$$I = \frac{V}{Z} = VY = 40\angle 0 \; Y$$

$$Y = Y_1 + Y_2 + Y_3$$

$$= \frac{1}{5+j12} + \frac{1}{3-j4} + \frac{1}{8}$$

$$= \frac{5-j12}{5^2+12^2} + \frac{3+j4}{3^2+4^2} + \frac{1}{8}$$

$$= (0.0296 - j0.07) + (0.12 + j0.16) + 0.125$$

$$= 0.274 + j0.084 = 0.28 \angle 17.9$$

$$\therefore I = VY = 11.55 \angle 17.9°$$

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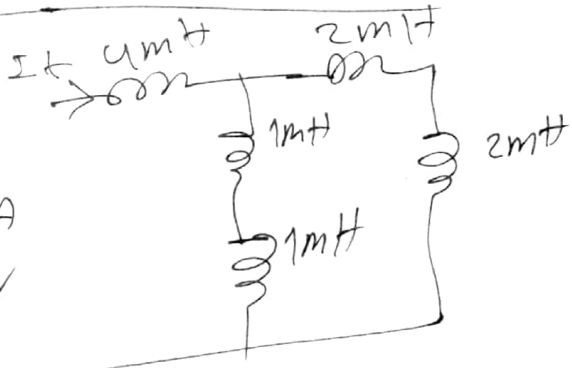
(9)



what freq. Produce $I_t = 500mA$ if $V_t = 10V$

$$Z = \frac{V}{I} = \frac{10}{500m} = 20$$

$$Z = jwL_{eq}$$

$$L_{eq} = \{(2m + 2m) // (1m + 1m)\} + 4m$$

$$= 5.33mH$$

$$\therefore |Z| = 2\pi f L_{eq} = 20$$

$$\therefore f = \frac{20}{2\pi \times 5.33 \times 10^{-3}} = 596.8 \text{ Hz}$$